

1) Find domain of definition:

a)  $z = \ln(y^2 - 4x + 8)$

b)  $z = \sqrt{9 - x^2 - y^2}$

c)  $z = \frac{\sqrt{4x - y^2}}{\ln(1 - x^2 - y^2)}$

d)  $z = \sqrt{x \cdot \sin y}$

2) Find partial derivatives:

a)  $z = x\sqrt{y} + \frac{y}{\sqrt{x}}$

b)  $z = x^y$

c)  $z = x^2y + y^2x + \ln y - e^x + 5$

d)  $u = (x)^{y \cdot z}$

e)  $e^z - xyz = 0$

3)  $z = \frac{y}{f(x^2 - y^2)}$ , where  $f$  is any differentiable function.

Prove, that  $\frac{1}{x} \cdot z'_x + \frac{1}{y} \cdot z'_y = \frac{z}{y^2}$ .

4) Find all partial derivatives of the second order.

$$z = x^3 + xy^2 - 5xy^3 + y^5$$

5) Find total differential of  $u$  if  $u = x^2 \cdot y + 3 \sin(2x + 5y) + x^3$ .

6) Find total differential of function  $\ln(x + 2y + 3z)$  at point  $M_0(1, 2, 0)$ .

7) Calculate approximately:

a)  $\ln\left(\sqrt[3]{1,03} + \sqrt[4]{0,98} - 1\right)$

b)  $(1,04)^{2,02}$ .