



## Syllabus Course Program



# Nonlinear Mechanics of Solid Deformed Body

### Specialty

113 – Applied Mathematics

### Institute

Institute of Computer Modeling, Applied Physics  
and Mathematics

### Educational program

Computer and Mathematical Modeling

### Department

Mathematical Modeling and Intelligent Computing  
in Engineering (161)

### Level of education

Master's level (1 year 4 months)

### Course type

Special (professional), Mandatory

### Semester

2

### Language of instruction

English

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## Lecturers and course developers



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[More about the lecturer on the department's website](#)

## General information

### Summary

"Nonlinear mechanics of a solid deformed body" is one of the fundamental disciplines in the preparation of a master's degree in applied mathematics. The first part includes the theory of elasticity, the second part is devoted to the theory of plates and shells. The applied value of these items is due to the fact that most of the disasters that occur are related to the insufficient strength of structures, when their individual elements stop performing their functions under the influence of load and lose their strength. Knowledge of such phenomena and the ability to resist them is mandatory for specialists who conduct applied research in various fields of the nonlinear mechanics of a solid deformed body.

### Course objectives and goals

The goal of the program is to equip students with the ability to solve complex specialized problems and practical problems of applied mathematics in professional activities or in the learning process, which involves the application of mathematical theories, methods, algorithms, information technologies and specialized software.

### Format of classes

Lectures, practical classes,  
consultations, self-study. Final control in the form of an exam.

## Competencies

GC7. Ability to think abstractly, analyse and synthesise.

PC2. Ability to conduct scientific research aimed to develop new and adapt existing mathematical and computer models to study various processes, phenomena and systems, conduct appropriate experiments and analyse the results.

PC4. Ability to develop and research mathematical and computer models, conduct computational experiments and solve formalised problems using specialised software.

PC9. The ability to mathematically formalise the formulation of scientific and practical problems, to choose a mathematical analytical or numerical method of its solution, which ensures the required accuracy and reliability of the result.

PC10. Ability to develop mathematical methods and algorithms for computer modelling of nonlinear physical phenomena and processes in innovative technological systems.

PC12. Ability to identify the essence of scientific and technical problems in professional activities, to apply appropriate mathematical models for the study of mechanical objects and processes.

## Learning outcomes

LO4. Build mathematical models of complex systems and choose methods of their research, implement the built models in software and check their adequacy using computer technologies.

LO16. Be able to develop mathematical methods and algorithms for computer modelling of nonlinear physical phenomena and processes in innovative technological systems.

## Student workload

The total volume of the discipline is 90 hours. (3 ECTS credits): lectures – 16 hours, laboratory work – 16 hours, independent work – 58 hours.

## Course prerequisites

Knowledge, skills, and previous courses that are necessary for successful course completion.

## Features of the course, teaching and learning methods, and technologies

The educational process includes: lectures using computer and information tools; practical classes, independent work. When teaching the lecture course, methods of problem-based learning are applied by applying such forms of learning as thematic and problem-based lectures. The purpose of such lectures is to develop students' logical and independent understanding of material.

Practical classes of meaningful modules are planned for each topic, include preparation for practical classes according to the specified plan; execution of control tasks; review of scientific publications on the selected issue. The following forms and methods of teaching are used: explanation, discussion, debate, writing theses, creating presentations, forming individual components of scientific works.

Students' independent work includes: preparation for practical classes, study of recommended scientific literature, writing reports, preparation for modular tests and assessment. Tasks of students' independent work are considered completed if they: are submitted within the specified time and are fully completed (reveal the topic of the task); do not have logical and calculation errors.

## Program of the course

### Topics of the lectures

Topic 1.

1.1. Material description of continuous environment.

1.2. Movement. The vector of displacement and speed of movement of a point.

Topic 2. Deformation. Gradients of deformation and displacements.

Green and Cauchy strain tensors. Logarithmic measures of deformation

Topic 3. Generalized deformation tensors and their main values.

Geometric equations.

Topic 4. Small deformation. Relative volume change during deformation. Cauchy formulas  
Topic 5. Mathematical statement of the problems of the theory of elasticity.

Topic 5. External forces. Equilibrium equations in projections onto local bases of the deformed state  
5.3. Solving problems of the theory of elasticity in displacements and stresses. Lamé and Beltrami-Mitchell equations.

Topic 6. Equilibrium equation in the initial basis. Piola-Kirghoff stress tensor

Topic 7. Potential energy of deformations.  
Energy stress tensor

Topic 8. Examples of deformed states. Affine transformation. Flat displacement field.

### **Topics of the workshops**

Topic 1. Fundamentals of tensor algebra in oblique angular coordinates. Covariant and contravariant components.

Topic 2. Approximation of deformation diagrams according to different models of materials.

Topic 3. Modeling of sample stretching at large deformations in the ANSYS software complex.

Topic 4. Modulation of nonlinear deformation in software complexes  
Polynomial model of the general form

Topic 5. Mooney-Rivlin model of hyperelastic material.

Topic 6. Numerical analysis of the deformation of thick-walled pipes made of hyperelastic materials.

Topic 7. Modeling of deformation of rubber shock absorbers

Topic 8. Numerical analysis of pneumatic shock absorbers.

### **Topics of the laboratory classes**

#### **Self-study**

Preparation for practical classes. Completion of mandatory homework

### **Course materials and recommended reading**

#### Basic literature

1. Lurie A. I., *Nonlinear Theory of Elasticity*, Paperback: North Holland, 2012. – 632p.
2. Божидарник В. В., Сулим Г. Т. *Елементи теорії пружності*, Львів: Світ, 1994. — 560 с.
3. *Nonlinear Elasticity: Theory and Applications* (London Mathematical Society Lecture Note Series No 282) / Editors Y.B. Fu, R.W. Ogden. Cambridge: Cambridge University Press, 2001. XI – 525 p.
4. Truesdell C., Noll W. *The Non-Linear Field Theories of Mechanics*. Third Edition. Berlin, Heidelberg, New York: Springer-Verlag, 2004. – 602 p.

#### Additional literature

1. Bar-Sinai Y., Librandi G., Bertoldi K., Moshe M. *Geometric charges and nonlinear elasticity of two-dimensional elastic metamaterials*// Northwestern University, Evanston, 2020. – 10195 – 10202p.

2. Zeidler E. Basic Equations of Nonlinear Elasticity Theory / Nonlinear Functional Analysis and its Applications. IV: Applications to Mathematical Physics, 1988. Springer - Verlag New York, Inc. P. 158 – 232.

## Assessment and grading

### Criteria for assessment of student performance, and the final score structure

To assess a student's performance, a point accumulation system is used. Maximum number of points for:

- independent work 5 points,
- control work 10 points,
- modular test 15 points.
- mandatory homework 20 points.

As an alternative to the cumulative point system, it is possible to take a written exam

### Grading scale

Total points	National	ECTS
90–100	Excellent	A
82–89	Good	B
75–81	Good	C
64–74	Satisfactory	D
60–63	Satisfactory	E
35–59	Unsatisfactory (requires additional learning)	FX
1–34	Unsatisfactory (requires repetition of the course)	F

## Norms of academic integrity and course policy

The student must adhere to the Code of Ethics of Academic Relations and Integrity of NTU "KhPI": to demonstrate discipline, good manners, kindness, honesty, and responsibility. Conflict situations should be openly discussed in academic groups with a lecturer, and if it is impossible to resolve the conflict, they should be brought to the attention of the Institute's management.

Regulatory and legal documents related to the implementation of the principles of academic integrity at NTU "KhPI" are available on the website: <http://blogs.kpi.kharkov.ua/v2/nv/akademichna-dobrochesnist/>

## Approval

Approved by

Date  
August 30, 2023

Head of the department  
Oleksii VODKA

Date  
August 30, 2023

Guarantor of the educational  
and professional program (1  
year 4 months)  
Oleksiy LARIN